

# A Denotational Engineering of Programming Languages

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Part 12: Lingua-OO Object-oriented programming  
(Not yet in the book)

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# Classes and objects intuitively

A class is a tuple of six components:

1. **directories** – catalogs of identifiers assigned to abstract members of a class; play an auxiliary role, (**katalogi**)
2. **type environment (T)** where identifiers are bound to:
  - a. *abstract types* ( $\Theta$ )
  - b. *concrete types* as in Lingua
3. **method environment (M)** where identifiers are bound to:
  - a. *abstract methods* or *signatures* which “announce” future procedures by their lists of formal parameters,
  - b. *concrete methods*, which are just procedures as in Lingua,
4. **class environment (C)** where identifiers are bound to:
  - a. *abstract classes* (NN) — some of their members are abstract,
  - b. *concrete classes* (NN) — all their members are concrete,
5. **valuation** where identifiers (called **attributes**) are bound to:
  - a. *abstract values* (pseudovales ( $\Omega$ , (bod, yok)))
  - b. *concrete values* (proper values (dat, (bod, yok));  $dat \neq \Omega$ )
6. **error register** as in Lingua-2

Types, methods, classes and values are called the **members** of a class.  
A concrete class is called an **object**.

# Classes formally

cla : Class	= Env x Store	
env : Env	= Dir x TypEnv x MetEnv x ClaEnv	environment
dir : Dir	= {[ ]}   Identifier $\Rightarrow$ Dir	directory (katalog)
tye : TypEnv	= Identifier $\Rightarrow$ Type   { $\Theta$ }	type environment
mee : MetEnv	= Identifier $\Rightarrow$ Method	method environment
cle : ClaEnv	= Identifier $\Rightarrow$ Class	class environment
sto : Store	= Valuation x (Error   {'OK'})	store
vat : Valuation	= Identifier $\Rightarrow$ Value	valuation

where:

met : Method	= Procedure   ProSig	method
pro : Procedure	= ImpPro   FunPro   TypPro	procedure
prs : ProSig	= FunProSig   ImpProSig   TypProSig	procedure signature
fps : FunProSig	= FoPaDe x TypExpDen	functional-procedure signature
ips : ImpProSig	= FoPaDe x FoPaDe	imperative-procedure signature
tps : TypProSig	= Identifier $^c$	topological-procedure signature
fpa : FoPaDe	= (Identifier x TypExpDen) $^{c^*}$	formal parameters

class = ((dir, tye, mee, cle), (vat, err))

In our model classes play the role of states!

# Classes and their directories

## directory

weight → []  
volume → []  
Shapes → "dir. of Shapes"  
p → []

## type environment

weight → Θ

sizes → (('L', ('A', number)), TT)

## method environment

volume → (val a, b, c, ref z)

area → (val a, b, ref y) {y:=a\*b}

## class environment

Shapes → "abstract class" }

Triangles → "concrete class" }

## valuation

a → (Ω, ('number'), TT)

b → (12, ('number'), value≤100))

Surface level (level 0) of a class

abstract members in red  
concrete members in black



Directories are redundancies

Directory lists all and only abstract members.

inner classes (has-a)  
of surface level  
classes of level 1

def: concrete class ≡ all elements concrete  
def: object = concrete class

**System Assumption** The well formedness of classes is an invariant of every transformation (mutation) of classes reachable in our algebra.

# Carriers of AlgDen-OO

## Applicative layer

ide	: Identifier	= ... somehow defined	identifiers
ded	: DatExpDen	= Class $\rightarrow$ Value   Error	data-expression denotations
ted	: TypExpDen	= Class $\mapsto$ Type   Error	type-expression denotations
tra	: TraExpDen	= Transfer	transfer-expression denotations
yok	: YokExpDen	= Yoke	yoke-expression denotations

## Imperative layer

ded	: DecDen	= Class $\mapsto$ Class	declarations (add new elements)
ind	: InsDen	= Class $\rightarrow$ Class	instruction (change values of attributes)
prd	: ProDen	= Class $\rightarrow$ Class	program denotations
fpa	: FoPaDe	= (Identifier $\times$ TypExpDen) $^{c^*}$	formal parameter denotations
apd	: AcPaDe	= Identifier $^{c^*}$	actual parameter denotations
tpd	: TypParDen	= Identifier $^{c^*}$	type parameters (formal and actual)
prs	: ProSig	= FunProSig   ImpProSig   TypProSig	procedure signatures
fps	: FunProSig	= FoPaDe $\times$ TypExpDen	
ips	: ImpProSig	= FoPaDe $\times$ FoPaDe	
tps	: TypProSig	= TypParDen	
pth	: Path	= {('empty')}   Identifier $^{c^*}$	paths

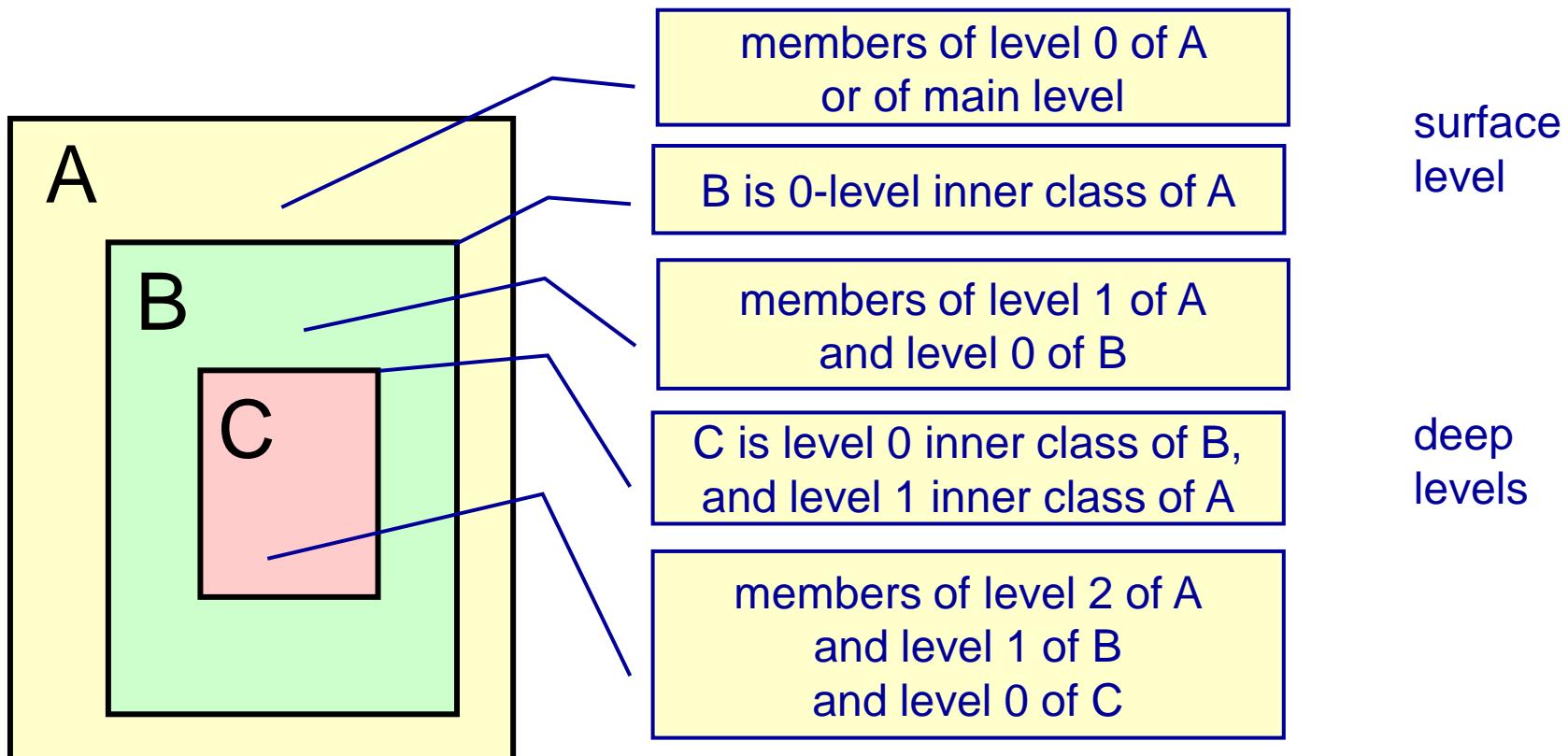
# Levels of a class

$A = ((\text{dir}, \text{tye}, \text{pre}, \text{cle}), (\text{vat}, \text{err}))$

0-level of A = members bound to identifiers in tye, pre, cle, vat

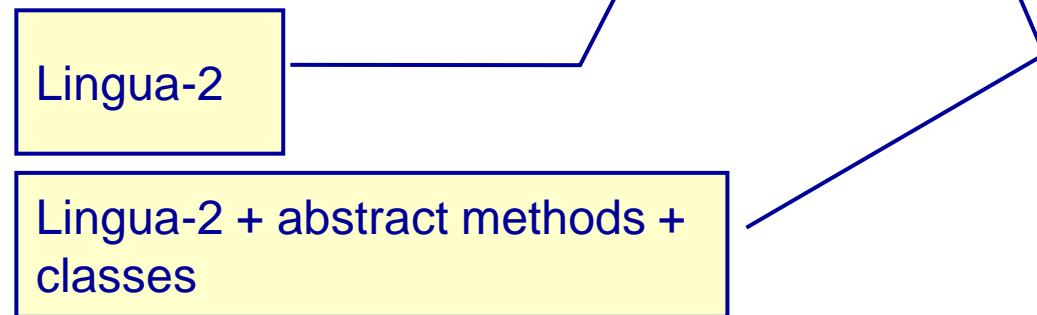
1-level of A = members bound to identifiers in inner classes of 0-level,  
etc. for  $n > 1$

**Note.** Members of level  $n$  do not belong to level  $n-1$ !



# Four categories of denotations

Lingua-OO	Applicative	Imperative
Surface	DatExpDen TypExpDen TraExpDen YokExpDen	DecDen InsDen ProDen
Deep	select + apply	select + apply + replace



Surface constructors = constructors of surface denotations

Deep constructors = constructors of deep denotations

Here "constructors" are understood in an algebraic sense.

# Surface Denotations and Their Constructors in AlgDen-OO

# Categories of surface constructors

## Basic assumptions:

- A. all attributes are private in their (directly) hosting classes,
  - B. all other members are public, although with restricted visibility,
  - C. instructions modify only the values of attributes (of an arbitrary level),
  - D. a program consists of a declaration followed by an instruction.
- recommended by  
} J.Jabłonowski.  
} J.Sroka

## Three categories of surface constructors:

1. old constructors in a new shape; they are said to be inherited from **Lingua-2**,
2. old constructors (slightly) modified: assignment and variable declaration,
3. (genuinely) new constructors.

Old constructors in a new shape create old denotations in a new shape:

$((\text{dir}, \text{tye}, \text{mee}, \text{cle}), (\text{vat}, \text{err}))$    $((\text{dir}, \text{tye-1}, \text{mee-1}, \text{cle}), (\text{vat-1}, \text{err-1}))$

old denotation in a new shape

## Old surface constructors in a new shape:

Constructors of data-expression denotations.

Constructors of type-expression denotations.

Constructors of declaration denotations **except variable declaration**.

Constructors of instruction denotations **except assignment**.

Constructors of program denotations.

# Surface variable declaration

declare-dat-var: Identifier x TypExpDen  $\mapsto$  DecDen i.e.

declare-dat-var: Identifier x TypExpDen  $\rightarrow$  Class  $\rightarrow$  Class

declare-dat-var.(ide, ted).cla =

is-error.clj → clj

`declared.ide.cla` → ‘identifier-declared’

**let**

typ = ted.clas

((dir, tye, mee, cle), (vat, 'OK')) = cla

typ : Error → cla ← typ

**true** → ((**dir**[ide/[ ]], tye, mee, cle), (**vat**[ide/(Ω, typ)], 'OK'))

A variable declaration always yields an abstract class.

# Surface assignment

assign : Identifier x DatExpDen  $\mapsto$  InsDen      i.e.

assign : Identifier x DatExpDen  $\mapsto$  Class  $\rightarrow$  Class

assign.(ide, ded).cla =

is-error.clj → class

**let**

((dir, tye, pre, cle), (vat, 'OK')) = cla

vat.ide = ? → cla ◀ 'identifier-not-declared'

`ded.clas = ?`       $\rightarrow$  ?      an infinite execution

ded.cla : Error → cla ← ded.cla

**let**

(dat-f, (bod-f, yok-f)) = vat.ide f – former

(dat-n, (bod-n, yok-n)) = ded.cla n – new

com = yok-f.(dat-n, bod-n)

com : Error → cla < com

bod-n ≠ bod-f → cla ◀ ‘inconsistent-bodies’

`com ≠ (tt, ('Boolean')) → cla ◀ 'yoke-not-satisfied'`

let

**val-n = ((dat-n, bod-n), yok-f)**

## ide is abstract

dir.ide = [ ]  ((dir[ide/?], tye, pre, cle), (vat[ide/val-n], 'OK'))

**true** → ((dir, tye, pre, cle), (vat[ide/val-n], 'OK'))

# Surface constructors for type- and method declarations

1. for declarations of abstract      types and methods,
2. for concretizations of abstract      types and methods,
3. for declarations of concrete      types and methods (inherited from **Lingua-2**).

# Types – decl. and concretizations of abstract t.

declare-abs-typ : Identifier  $\rightarrow$  DecDen

concretize-abs-typ : Identifier x TypExpDen  $\rightarrow$  DecDen

declare-abs-typ.ide.cla =

is-error.cla  $\rightarrow$  cla

ide : declared.cla  $\rightarrow$  'identifier-declared'

let

((dir, tye, mee, cle), (vat, err)) = cla

true  $\rightarrow$  ((dir[ide/[ ]], tye[ide/ $\Theta$ ], mee, cle), (vat, err))

a pseudotype

concretize-abs-typ.(ide, ted).cla =

is-error.cla  $\rightarrow$  cla

let

((dir, tye, mee, cle), (vat, err)) = cla

tye.ide = ?  $\rightarrow$  'abstract-type-unknown'

tye.ide  $\neq \Theta$   $\rightarrow$  'an-abstract-type-expected'

let

typ = ted.cla

typ : Error  $\rightarrow$  cla  $\blacktriangleleft$  error.cla

true  $\rightarrow$  ((dir[ide/?], tye[ide/typ], mee, cle), (vat, err))

only abstract types may be concretized

# Methods – declarations of abstract m.

declare-imp-sig : Identifier x ImpProSig  $\rightarrow$  DecDen      i.e.

declare-imp-sig : Identifier x ImpProSig  $\rightarrow$  Class  $\mapsto$  Class

declare-imp-sig.(ide, ips).cla =

is-error.cla                   $\rightarrow$  cla

declared.ide.cla             $\rightarrow$  'identifier-declared'

**let**

((dir, tye, mee, cle), (vat, 'OK')) = cla

**not** no-repetition.ips  $\rightarrow$  cla  $\blacktriangleleft$  'repetitions-of-formal-parameters'

**true**                         $\rightarrow$  ((dir[ide/[ ]], tye, mee[ide/ips], cle), (vat, 'OK'))

declare-fun-sig : Identifier x FunProSig  $\rightarrow$  Class  $\mapsto$  Class

declare-fun-sig.(ide, fps).cla =

is-error.cla                   $\rightarrow$  cla

declared.ide.cla             $\rightarrow$  'identifier-declared'

**let**

((dir, tye, mee, cle), (vat, 'OK')) = cla

**not** no-repetition.fps  $\rightarrow$  cla  $\blacktriangleleft$  'repetitions-of-formal-parameters'

**true**                         $\rightarrow$  ((dir[ide/[ ]], tye, mee[ide/fps], cle), (vat, 'OK'))

analogous to  
imperative

# Concretizations of abstract imperative methods

concretize-imp-sig : Identifier x FoPaDe x FoPaDe x ProDen  $\mapsto$  DecDen      i.e.

concretize-imp-sig : Identifier x FoPaDe x FoPaDe x ProDen  $\mapsto$  Class  $\mapsto$  Class

concretize-imp-sig.(ide, fpa-v, fpa-r, prd).cla =

is-error.cla

→ cla

**not** ide : declared.cla

→ 'identifier-unknown'

mee.ide = ?

→ 'no-such-method'

dir.ide = ?

→ 'method-already-concrete'

**let**

message

= no-repetitions.(fpd  $\subseteq$  fpd-r)

((dir, tye, mee, cle), (vat, 'OK'))

= cla

(fpa-vs, fpa-rs)

= mee.ide

- a signature of ide

message  $\neq$  'OK'

→ cla  $\blacktriangleleft$  message

fpa-vs  $\neq$  fpa-v

→ cla  $\blacktriangleleft$  'value-parameters-not-compatible'

fpa-rs  $\neq$  fpa-r

→ cla  $\blacktriangleleft$  'reference-parameters-not-compatible'

**let**

P = create-imp-pro.((fpa-v, fpa-r, prd), (dir, tye, mee[ide/P], cle))    fixed-point def.

true

→ ((dir[ide/?], tye, mee[ide/P], cle), (vat, 'OK'))

The case of  
functional methods is  
analogous

**Note:** Procedures may create their private temporary classes.

# Declarations of classes

by a path

1. selecting an inner class of an input class, which in particular may be also the input class itself or an empty class,
2. modifying that class by a given OO-program,
3. binding the new class to a given identifier in the input class.

# Surface declarations of classes

dec-class : Identifier x Path x ProDen  $\mapsto$  DecDen      i.e.

dec-class : Identifier x Path x ProDen  $\mapsto$  Class  $\mapsto$  Class

dec-class.(ide, pat, prd).ho-cla =  
is-error.ho-cla       $\rightarrow$  ho-cla

hosting class  
k. goszcząca

ide : declared.ho-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  'class-name-declared'

**let**

in-cla = select-cla.pat.ho-cla      the parent inner class

is-error.in-cla       $\rightarrow$  in-cla      in that case in-cla = ho-cla

**let**

dec-cla = prd.in-cla      the declared class

is-error.dec-cla       $\rightarrow$  ho-cla  $\blacktriangleleft$  error.dec-cla

**let**

((dec-dir, dec-tye, dec-mee, dec-cle), (dec-vat, 'OK')) = dec-cla

((ho-dir, ho-tye, ho-mee, ho-cle), (ho-vat, 'OK')) = ho-cla

dec-dir = []       $\rightarrow$  ((ho-dir, ho-tye, ho-mee, ho-cle[ide/dec-cla]), (ho-vat, 'OK'))

true       $\rightarrow$  ((ho-dir[ide/dec-dir], ho-tye, ho-mee, ho-cle[ide/dec-cla]), (ho-vat, 'OK'))

declared class is abstract

If pat = ('empty') we construct the declared class "from scratch".

Two ways of introducing inner classes into a declared class:  

- by inheritance,
- by declaration.

# Auxiliary Deep Constructors not in AlgDen-OO

# Categories of deep constructors

all these constructors have an auxiliary character, i.e.  
they will not become constructors in AlgDen-OO

no syntactic representation  
available to programmers

s-select-cl	: Identifier	→ Class → Class	s- surface
select-cl	: Path	→ Class → Class	
s-remove-cl	: Identifier	→ Class → Class	
remove-cl	: Path	→ Class → Class	
s-insert-cl	: Identifier x Class	→ Class → Class	
insert-cl	: Path x Identifier x Class	→ Class → Class	
replace-cl	: Path x Class	→ Class → Class	

deep constructors  
are defined  
inductively starting  
from from surface  
constructors

# Selecting a surface inner-class

Selecting a class which is a level 1 class of a given class

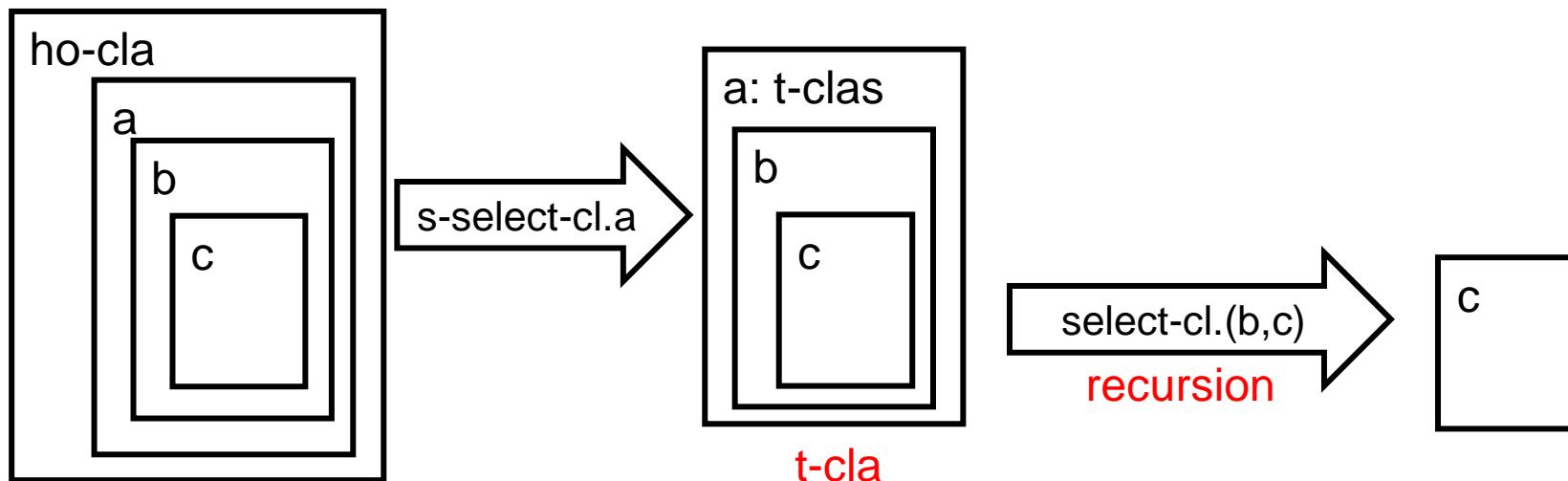
s-select-cl : Identifier  $\mapsto$  Class  $\mapsto$  Class

s-select-cl.ide.ho-cla =  
is-error.ho-cla  $\rightarrow$  ho-cla  
**let**  
((dir, tye, mee, cle), (vat, err)) = cla  
cle.ide = ?  $\rightarrow$  ho-cla  $\blacktriangleleft$  'no-such-class'  
**true**  $\rightarrow$  cle.ide

# Deep class selection

Selecting a class at the end of a path

`select.(a,b,c).ho-cla`



# Deep class selection

Selecting a class at the end of a path

select-cl : Path  $\mapsto$  Class  $\mapsto$  Class

select-cl.pat.ho-cla =

is-error.ho-cla  $\rightarrow$  ho-cla

pat = ('empty')  $\rightarrow$  ([], [], []), ([], 'OK')      an empty class

pat = ()  $\rightarrow$  ho-cla

**let**

ide = top.pat

p-pat = pop.pat

t-cla = s-select-cl.ide.cla

is-error.t-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  error.t-cla

**true**  $\rightarrow$  **select-cl.p-pat.t-cla**

recursion

# Removing a surface inner-class

Removing a class which is level 1 class of a given class

s-remove-cl : Identifier  $\mapsto$  Class  $\mapsto$  Class

s-remove-cl.ide.ho-cla =

is-error.ho-cla  $\rightarrow$  ho-cla

**let**

((dir, tye, mee, cle), (vat, err)) = ho-cla

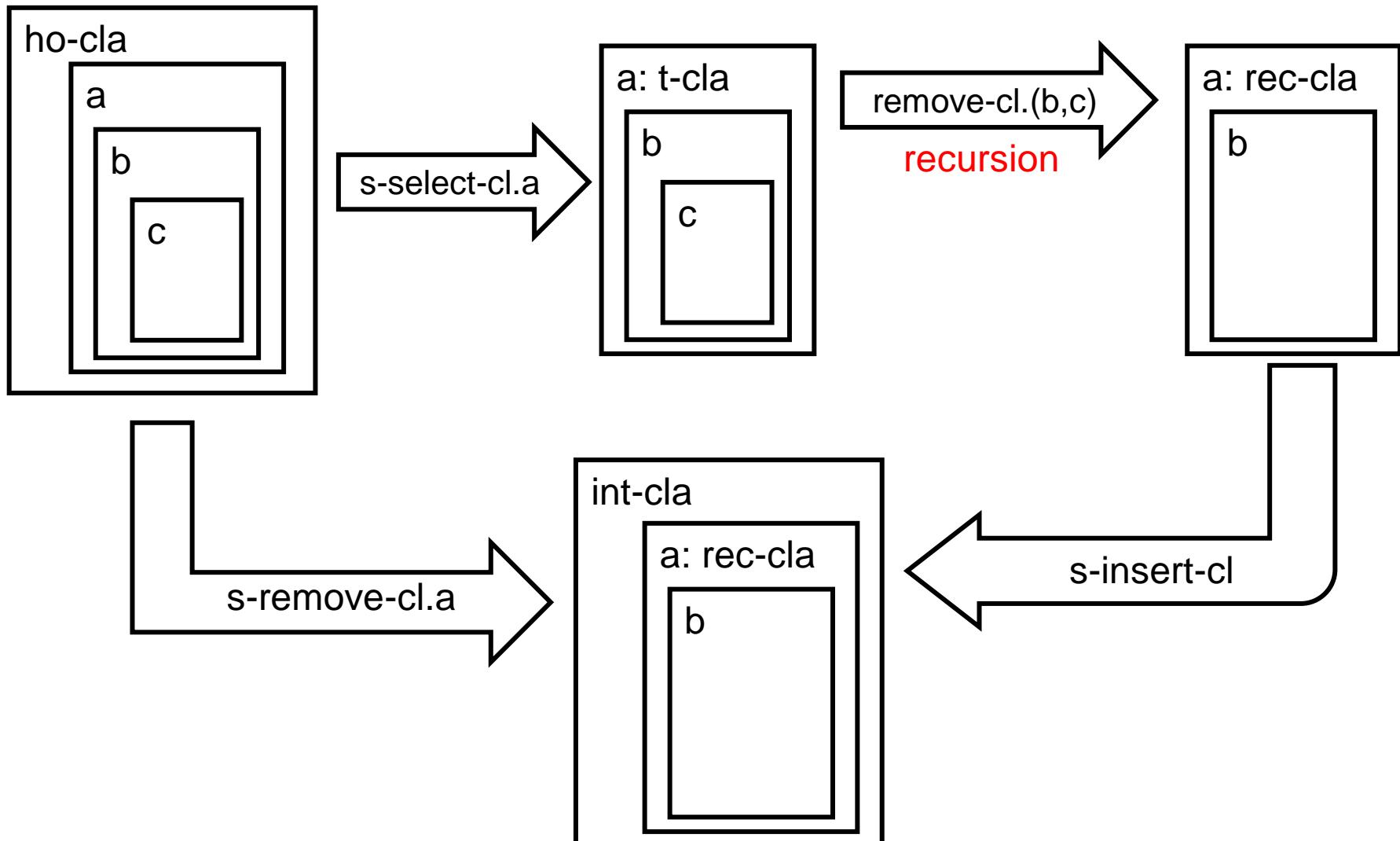
cle.ide = ?  $\rightarrow$  ho-cla  $\blacktriangleleft$  'no-such-class'

dir.ide = ?  $\rightarrow$  ((dir, tye, mee, cle[ide/?]), (vat, err))      concrete-class removal

true  $\rightarrow$  ((dir[ide/?], tye, mee, cle[ide/?]), (vat, err)) abstract-class removal

# Deep class removal

Removing a class at the end of a path  
 $\text{remove-cl.}(a,b,c).\text{ho-cla}$



# Deep class removal

Removing a class at the end of a path

remove-cl : Path  $\mapsto$  Class  $\mapsto$  Class

remove-cl.pat.ho-cla =

is-err.ho-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  'empty-class-cannot-be-removed'

pat = ('empty')  $\rightarrow$  ho-cla

pat = ()  $\rightarrow$  ho-cla  $\blacktriangleleft$  'empty-path'

a class can't be removed from itself

**let**

ide = top.pat

p-pat = pop.pat

t-cla = s-select-cl.ide.ho-cla

a top class

is-error.t-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  error.t-cla

**let**

int-cla = s-remove-cl.ide.ho-cla

intermediate class

is-error.int-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  error.int-cla

p-pat = ()  $\rightarrow$  int-cla

**let**

rec-cla = remove-cl.p-pat.t-cla

recursion

is-error.rec-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  error.rec-cla

**true**  $\rightarrow$  s-insert-cl.(ide, rec-cla).int-cla

# Inserting a surface class

Inserting a class which becomes level 1 class of a given class

s-insert-cl : Identifier x Class  $\mapsto$  Class  $\mapsto$  Class

s-insert-cl.(ide, in-cla).ho-cla =

is-error.ho-cla  $\rightarrow$  ho-cla

is-error.in-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  error.in-cla

ide : declared.ho-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  'identifier-already-declared'

let

((dir-in, tye-in, mee-in, cle-in), (vat-in, 'OK')) = in-cla

((dir-ho, tye-ho, mee-ho, cle-ho), (vat-ho, 'OK')) = ho-cla

dir-in = [ ]  $\rightarrow$  ((dir-ho, tye-ho, mee-ho, cle-ho[ide/in-cla]), (vat-ho, 'OK'))

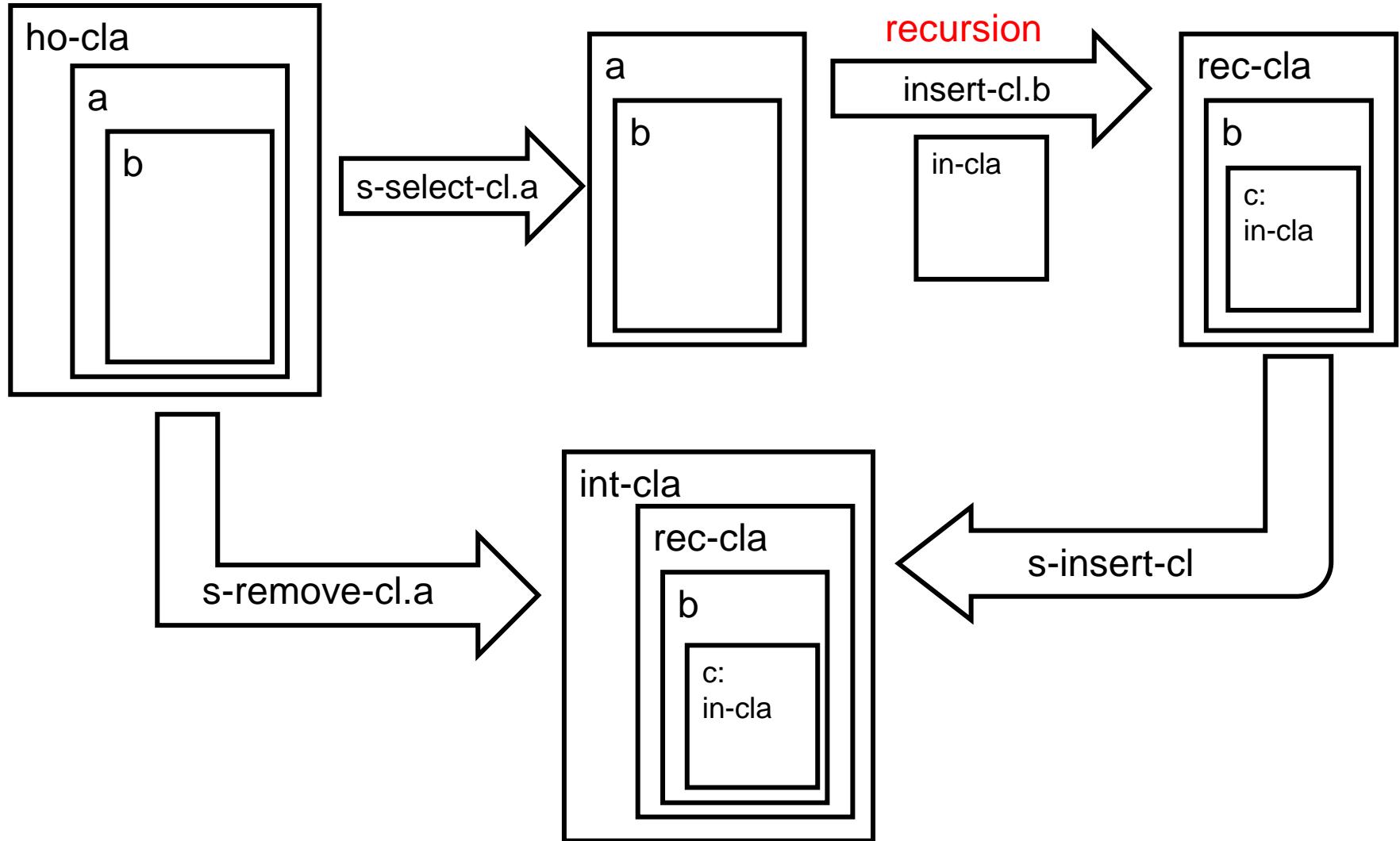
true  $\rightarrow$  ((dir-ho[ide/dir-in], tye-ho, mee-ho, cle-ho[ide/in-cla]), (vat-ho, 'OK'))

in-cla is concrete

# Deep class insertion

Inserting a class at the end of a path

insert-cl.((a,b), c, in-cla).ho-cla



# Deep class insertion

## Inserting a class at the end of a path

$\text{insert-cl} : \text{Path} \times \text{Identifier} \times \text{Class} \rightarrow \text{Class} \rightarrow \text{Class}$

$\text{insert-cl}(\text{pat}, \text{ide}, \text{in-cla}).\text{ho-cla} =$

$\text{is-error.ho-cla} \rightarrow \text{ho-cla}$

$\text{is-error.in-cla} \rightarrow \text{ho-cla} \blacktriangleleft \text{error.in-cla}$

$\text{pat} = (\text{'empty'}) \rightarrow \text{ho-cla} \blacktriangleleft (\text{'empty'})\text{-path-not-allowed'}$

$\text{pat} = () \rightarrow \text{s-insert-cl}(\text{ide}, \text{in-cla}).\text{ho-cla}$

**let**

$\text{top-ide} = \text{top.pat}$

$\text{p-pat} = \text{pop.pat}$

$\text{t-cla} = \text{s-select-cl}.\text{top-ide}.\text{ho-cla}$

top class

$\text{int-cla} = \text{s-remove-cl}.\text{top-ide}.\text{ho-cla}$

intermediate class

$\text{is-error.t-cla} \rightarrow \text{ho-cla} \blacktriangleleft \text{error.t-cla}$

$\text{is-error.int-cla} \rightarrow \text{ho-cla} \blacktriangleleft \text{error.int-cla}$

**let**

$\text{rec-cla} = \text{insert-cl}(\text{p-pat}, \text{ide}, \text{int-cla}).\text{t-cla}$

recursion

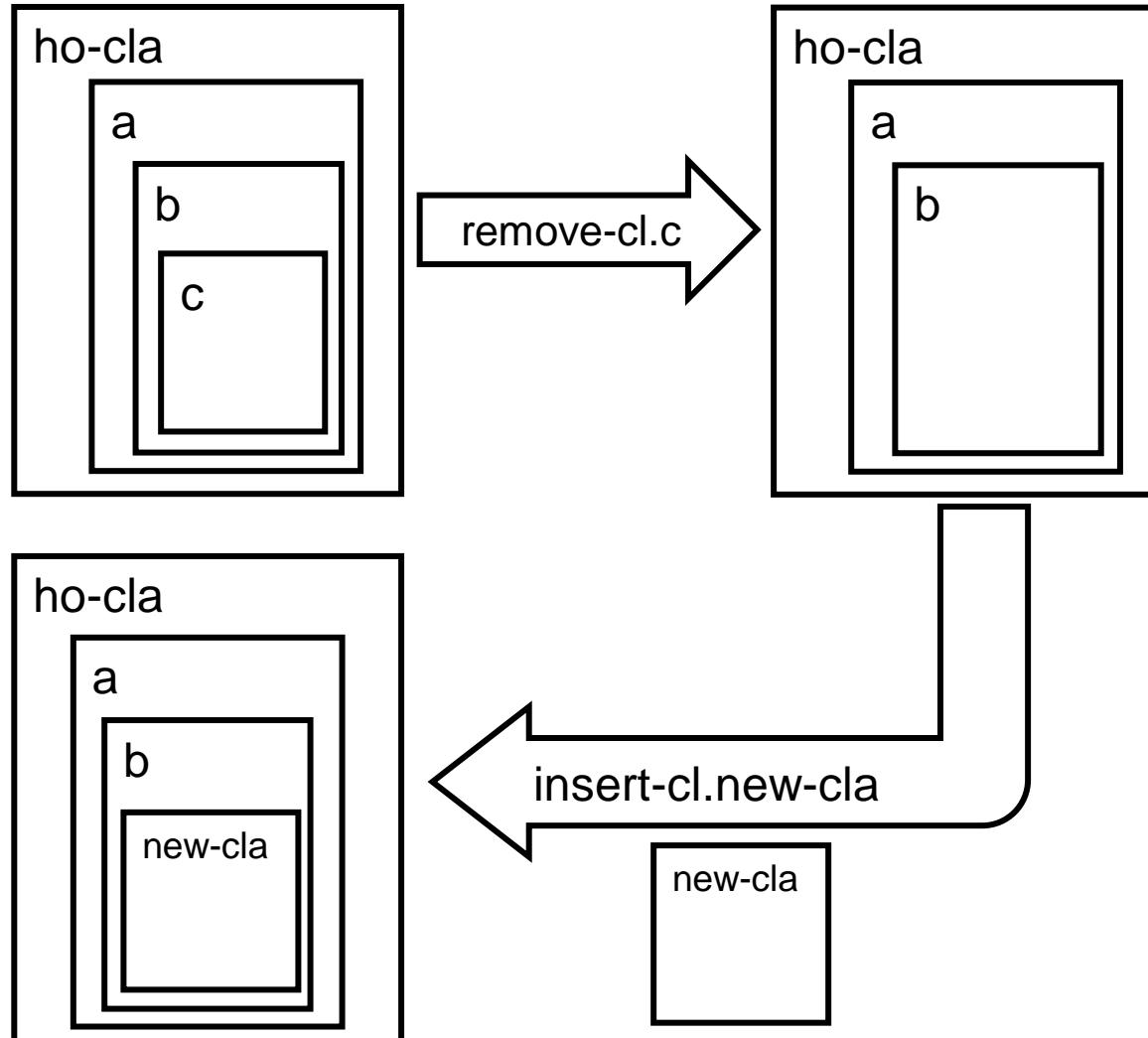
$\text{is-error.rec-cla} \rightarrow \text{ho-cla} \blacktriangleleft \text{error.rec-cla}$

$\text{true} \rightarrow \text{s-insert-cl}(\text{ide}, \text{rec-cla}).\text{int-cla}$

# Deep class replacement

Replacing a class at the end of a path

replace-cl.((a,b), c, new-cla).ho-cla



# Deep class replacement

A general scheme: remove + insert.

replace-cl : Path x Class  $\mapsto$  Class  $\mapsto$  Class

Replacement of a class at the end of a path by a new class.

replace-cl.(pat, new-cla).ho-cla =

is-error.ho-cla  $\rightarrow$  ho-cla

is-error.new-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  error.new-cla

pat = ('empty')  $\rightarrow$  ho-cla  $\blacktriangleleft$  ('empty)-path-not-allowed'

pat = ( )  $\rightarrow$  ho-cla  $\blacktriangleleft$  'empty-path'

**let**

ide = last.pat

sh-pat = skip-last.pat short path

int-cla = remove-cl.pat.ho-cla intermediate class

is-error.int-cla  $\rightarrow$  ho-cla  $\blacktriangleleft$  error.int-cla

**true**  $\rightarrow$  insert.(sh-pat, ide, new-cla).int-cla

# Surface constructors used at a depth

# A universal operator select + modify + replace

ope : Class → Class

deep.ope : Path ↠ Class → Class

deep.ope.pat.ho-cla =

is-error.ho-cla → ho-cla

pat = ('empty') → ho-cla ◀ ('empty')-path-not-allowed'

pat = () → ho-cla ◀ 'empty-path'

**let**

so-cla = select.pat.ho-cla      source class

is-error.so-cla → ho-cla ◀ error.so-cla

**let**

mod-cla = ope.so-cla      modified class

is-error.mod-cla → ho-cla ◀ error.mod-cla

true → replace-cl.(pat, mod-cla).ho-cla

Ten operator pozwala zdefiniować konstruktory odpowiadające głębokiemu wykonaniu dowolnych denotacji powierzchniowych. W szczególności możemy na dowolnej głębokości przekształcić całą klasę dowolnym OO-programem. Czy taką możliwość chcemy dać do ręki programiście?

# Setter – a surface-to-deep instruction

set : Path x Identifier x DatExpDen  $\mapsto$  InsDen      i.e.

set : Path x Identifier x DatExpDen  $\mapsto$  Class  $\rightarrow$  Class

set.(pat, ide, ded).ho-cla =

is-error.ho-cla  $\rightarrow$  ho-cla

**let**

ta-cla = select.pat.ho-cla

is-error.ta-cla  $\rightarrow$  ta-cla

ded.ho-cla = ?  $\rightarrow$  ?

**let**

val = ded.ho-cla

val : Error  $\rightarrow$  ho-cla  $\blacktriangleleft$  val

**let**

((ta-dir, ta-tye, ta-pre, ta-cle), (ta-sto, 'OK')) = ta-cla

ta-sto.ide = ?  $\rightarrow$  'no-such-attribute'

**let**

ca-cla = ((ta-dir, ta-tye, ta-pre, ta-cle), (ta-sto[ide/val], 'OK')) concrete attribute

aa-cla = ((ta-dir[ide/ ?], ta-tye, ta-pre, ta-cle), (ta-sto[ide/val], 'OK')) abst. attr.

ta-dir.ide = ?  $\rightarrow$  replace-cl.(pat, ca-cla).ho-cla

**true**  $\rightarrow$  replace-cl.(pat, aa-cla).ho-cla

Sets a value computed in  
a hosting class to an  
attribute of a deep class.

target class

in this case ta-cla = ho-cla

pat = ()

- surface assignment

pat = ('empty')

- yields a simple concrete class

# Getters – deep-to-surface expressions

A general scheme: select + evaluate

## data getter

$d\text{-get} : \text{Path} \times \text{DatExpDen} \rightarrow \text{Class} \rightarrow \text{DatExpDen}$  i.e.

$d\text{-get} : \text{Path} \times \text{DatExpDen} \rightarrow \text{Class} \rightarrow \text{Value} \mid \text{Error}$

$d\text{-get}(\text{pat}, \text{ded}).\text{ho-cla} = \text{ded}.\text{(select-cl.pat.ho-cla)}$

## type getter

$t\text{-get} : \text{Path} \times \text{TypExpDen} \rightarrow \text{Class} \rightarrow \text{TypExpDen}$  i.e.

$t\text{-get} : \text{Path} \times \text{TypExpDen} \rightarrow \text{Class} \rightarrow \text{Value} \mid \text{Error}$

$t\text{-get}(\text{pat}, \text{ted}).\text{ho-cla} = \text{ted}.\text{(select-cl.pat.ho-cla)}$

Expression represented by ded/ted is evaluated in an inner class of cla indicated by the path pat.

Both constructions include deep calls of functional/typological procedures.

# Deep call of a procedure

call-imp-proc : Identifier x AcPaDe x AcPaDe  $\mapsto$  Class  $\rightarrow$  Class

deep-call-imp-proc : Path x Identifier x AcPaDe x AcPaDe  $\mapsto$  Class  $\rightarrow$  Class

deep-call-imp-proc.(pat, ide, apd-v, apd-r).cla =

call-imp-proc.(ide, apd-v, apd-r).(select-cl.pat.cla)

This means that

call-imp-proc.(ide, apd-v, apd-r)

is executed in the deep class

deep-cla = select.pat.cla

Consequently:

- ide must be declared in deep-cla,
- actual parameters are computed in deep-cla.

If we want to pass actual parameters stored in the main-class store to a deep procedure call, we have to export them via setters to the deep class.

I na tym na razie koniec  
c.d.n.